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Math\_Questions\_0022

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1) Graph the function  $f(x) = 8/(x^2+4)$

Show all work. State the domain, calculate the limit as  $x \rightarrow \pm \infty$ , clearly state all relative max/min pts and any inflection pts, indicate intervals upon which  $f$  is increasing/decreasing, concave up/down. Sketch.

2) a) Explain what it means to say that  $g(x)$  is continuous at  $x$ .

b) Explain what it means to say that  $g(x)$  is differentiable at  $x = a$ .

c) Let  $g(x) = \begin{cases} ax^2 + b & \text{for } x \leq 1 \\ 2x^3 & \text{for } x > 1 \end{cases}$

Determine the values of  $a$  and  $b$  so that  $g$  is differentiable (and hence continuous)

3) A drilling rig 12 miles offshore is to be connected by a pipe to a refinery onshore, 20 miles down the coast from the rig. If underwater pipe costs \$50,000 per mile and land-based pipe costs \$30,000 per mile, what values of  $x$  and  $y$  give the least expensive connection?

4) Coffee is draining from a conical filter into a cylindrical coffeepot at the rate of 10 cubic inches/minute. How fast is the level in the pot rising when the coffee in the cone is 5 inches deep? How fast is the level in the cone falling then? [Recall: volume of a cylinder =  $\pi r^2 h$  and volume of a cone =  $\pi/3 r^2 h$ ] Hint: use proportional/similar triangles.

Diagram shows that the cylinder and cone both have diameter 6 inches, and the cone has height 6 inches

5) The annual world rate of water use  $t$  years after 1960, for  $t \leq 35$ , was approximately  $860 e^{0.04 t}$  cubic kilometers per year. How much water was used between 1960 and 1995?