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**Math\_Questions\_0046**

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1. What is the domain of the function  $f(t) = \frac{\sqrt{t^2 - 1}}{t - 3}$ ?

2.

Find the indicated composite function:  $f(x + 3)$ , where  $f(x) = x^3 + 2$ .

A)  $x^3 + 5$    B)  $x^3 + 6$    C)  $(x + 3)^3 + 2$    D)  $x^3 + x + 5$

3.

An efficiency study of the morning shift at a certain factory indicates that an average worker who arrives on the job at 8:00 A.M. will have assembled

$f(x) = -x^3 + 5x^2 + 16x$  transistor radios  $x$  hours later. How many radios will such a worker assemble between 10:00 and 11:00 A.M.?

A) 20   B) 22   C) 15   D) 18

4. Find  $f(2)$  where  $f(x) = \begin{cases} x^2 - 1 & \text{if } x < 1 \\ 3 & \text{if } x = 1 \\ 2 - 5x & \text{if } x > 1 \end{cases}$

5.

True or False: The domain of  $f(x) = \frac{x + 1}{x^2 - 1}$  is all  $x$  except 1.

A) True

B) False

6. A manufacturer of self-baiting mousetraps is currently selling 1,500 traps a month to retailers at a price of \$1 per trap. She estimates that for each 5 cent increase in price, she will sell 25 fewer traps per month. Her costs consist of a fixed overhead of \$180 a month and 30 cents per trap for labor and materials. Find the dollar profit  $P(x)$  as a function of the price  $x$ . Estimate the value of  $x$  where the maximum occurs from the graph.

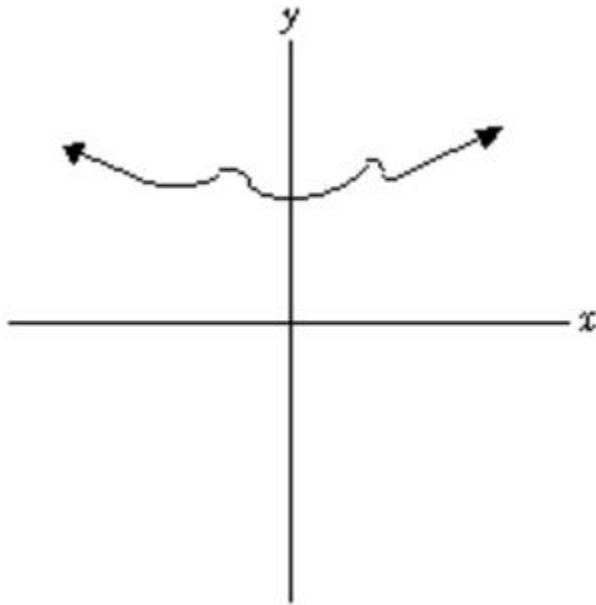
7. An apartment complex in a small college town has 120 units total. If they charge \$1200 per month, they can rent every apartment, but each \$50 increase in rent will result in 3 vacant apartments. Find the price they should charge to maximize their revenue. (Hint: Write a function describing revenue in terms of monthly rent, then find the vertex).

8. The cost of renting a backhoe at one distributor is \$320, plus \$35 per day. Write a linear function  $C(x)$  that describes the cost of renting the backhoe for  $x$  days, then use your function to find how much it would cost to rent it for 20 days.

- A)  $C(x) = 320x + 35$ ; \$6,435      C)  $C(x) = 320 + 35x$ ; \$1,020  
 B)  $C(x) = 20(320 + 35x)$ ; \$20,400      D)  $C(x) = 35x + 300$ ; \$1000

9.

True or False: The first derivative of a function is graphed below. The function has at least one relative extrema.



- A) True  
 B) False

10. Find the limit:  $\lim_{x \rightarrow 4} \frac{\sqrt{x} - 2}{x - 4}$

- A) Does not exist    B) 4    C)  $-\frac{1}{4}$     D)  $\frac{1}{4}$

11. Find all the values of  $x$  for which the function is not continuous.  $f(x) = \begin{cases} x^2 + 4 & \text{if } x \leq 5 \\ 4 & \text{if } x > 5 \end{cases}$

12. Find the equation of the tangent line to the curve  $f(x) = \frac{4}{x} - x$  at the point where  $x = 1$

13.

The equation of the line tangent to the graph of  $f(x) = 3\sqrt{x}$  at  $x = 1$  is

A)  $y = \frac{1}{2}x - \frac{1}{2}$    B)  $y = \frac{1}{2}x + \frac{1}{2}$    C)  $y = \frac{3}{2}x + \frac{3}{2}$    D)  $y = \frac{3}{2}x - 1$

14. A manufacturer can produce radios for \$10 apiece. It is estimated that if the radios are sold for  $x$  dollars apiece, consumers will buy  $100 - x$  of them each month. Use calculus to determine the price in dollars at which profit will be greatest.

15. For  $f(x) = 18 - x^2$ , find the slope of the secant line connecting the points whose  $x$ -coordinates are  $x = -5$  and  $x = -4.9$ . Then use calculus to find the slope of the line that is tangent to the graph of  $f$  at  $x = 5$ .

16.

True or False: Differentiating  $f(x) = \frac{1}{3}x^7 - 2x^5 + 9x - 8$  gives  $\frac{7x^6}{3} - 10x^4 + 9$ .

- A) True
- B) False

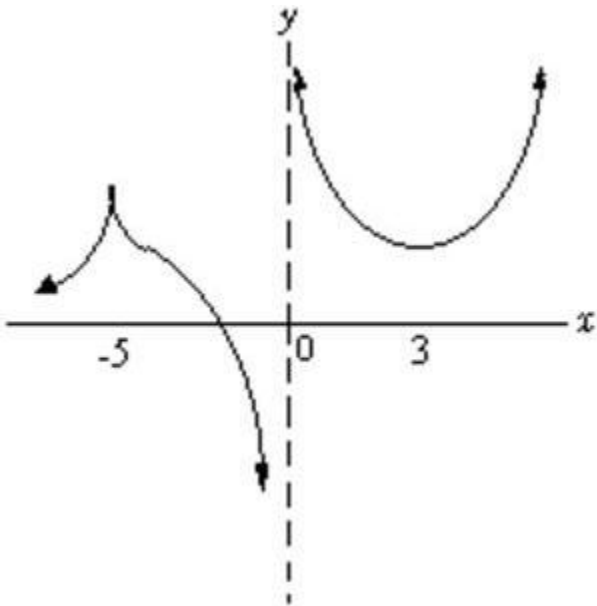
17.

An appliance store estimates that they can sell  $R(x)$  refrigerators in a month according to the formula  $R(x) = -0.01x^3 + x^2 - 3x + 200$  where  $x$  is the number of television ads they run per day. Find  $R'(4)$  and interpret what it tells us about sales.

- A)  $R'(4) = 203.36$ ; they'll sell about 203 refrigerators if they run 4 ads per day.
- B)  $R'(4) = 4.52$ ; they'll sell about 5 refrigerators if they run 4 ads per day.
- C)  $R'(4) = 4.52$ ; sales will be increasing at about 5 refrigerators per month per ad when they're running 4 ads.
- D)  $R'(4) = 203.36$ ; the cost of refrigerators will be rising by \$203.36 if they're selling 4 per day.

18.

Find all intervals where the derivative of the function shown below is negative.



19.

A small manufacturing company estimates that the total cost in dollars of producing  $x$  radios per day is given by the formula  $C = 0.1x^2 + 20x + 500$ . Find the number of units that will minimize the average cost.

A) 100 B) 147 C) 36 D) 71

20.

A 5-year projection of population trends suggests that  $t$  years from now, the population of a certain community will be  $P(t) = -t^3 + 12t^2 + 144t + 55$  thousand.

1) At what time during the 5-year period will the population be growing most rapidly?

2) At what time during the 5-year period will the population be growing least rapidly?

3) At what time is the rate of population growth changing most rapidly?

A)  $t = 4$  years;  $t = 0$  years;  $t = 0$  years      C)  $t = 4$  years;  $t = 3$  year;  $t = 5$  years

B)  $t = 0$  years;  $t = 0$  years;  $t = 4$  years      D)  $t = 4$  years;  $t = 0$  years;  $t = 4$  years

21.

If the demand for a commodity is  $D(p) = 146 - 2p - 4p^2$  and the average cost is  $A(x) = 1 + \frac{1}{x}$ ,

find the maximum profit