

## TABLE of INTEGRALS

$$\int x^a dx = \frac{1}{a+1} x^{a+1} + C, \quad a \neq -1 \quad \int \frac{1}{x} dx = \ln|x| + C = \ln|kx|, \quad C = \ln k$$

$$\int e^{ax} dx = \frac{1}{a} e^{ax} + C \quad \int a^x dx = \frac{1}{\ln a} a^x + C, \quad a \neq 1$$

$$\int \sin x dx = -\cos x + C \quad \int \cos x dx = \sin x + C$$

$$\int \sec^2 x dx = \tan x + C \quad \int \operatorname{cosec}^2 x dx = -\cot x + C$$

$$\int \tan x dx = \ln|\sec x| + C \quad \int \cot x dx = \ln|\sin x| + C$$

$$\int \sec x dx = \ln|\sec x + \tan x| + C \quad \int \operatorname{cosec} x dx = \ln|\operatorname{cosec} x - \cot x| + C$$

$$\int \sinh x dx = \cosh x + C \quad \int \cosh x dx = \sinh x + C$$

$$\int \operatorname{sech}^2 x dx = \tanh x + C \quad \int \operatorname{cosech}^2 x dx = -\coth x + C$$

$$\int \frac{dx}{1+x^2} = \tan^{-1} x + C, \quad a > 0 \quad \int \frac{dx}{1-x^2} = \frac{1}{2} \ln \left| \frac{1+x}{1-x} \right| + C, \quad x^2 \neq 1$$

$$\int \frac{dx}{1-x^2} = \tanh^{-1} x + C, \quad |x| < 1 \quad \int \frac{dx}{1-x^2} = \operatorname{coth}^{-1} x + C, \quad |x| > 1$$

$$\int \frac{dx}{\sqrt{1-x^2}} = \sin^{-1} x + C = -\cos^{-1} x + C', \quad |x| \leq 1$$

$$\int \frac{dx}{\sqrt{x^2+1}} = \sinh^{-1} x + C = \ln(x + \sqrt{x^2+1}) + C'$$

$$\int \frac{dx}{\sqrt{x^2-1}} = \cosh^{-1} x + C = \ln(x + \sqrt{x^2-1}) + C' \quad x \geq 1$$

$$\begin{aligned} I_{m,n} = \int \sin^m x \cos^n x dx &= \frac{\sin^{m+1} x \cos^{n-1} x}{m+n} + \frac{n-1}{m+n} I_{m,(n-2)} \\ &= -\frac{\sin^{m-1} x \cos^{n+1} x}{m+n} + \frac{m-1}{m+n} I_{(m-2),n} \end{aligned}$$